

# Consensus sequence Zen

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**Abstract:** Consensus sequences are widely used in molecular biology but they have many flaws. As a result, binding sites of proteins and other molecules are missed during studies of genetic sequences and important biological effects cannot be seen. Information theory provides a mathematically robust way to avoid consensus sequences. Instead of using consensus sequences, sequence conservation can be quantitatively presented in bits of information by using sequence logo graphics to represent the average of a set of sites, and sequence walker graphics to represent individual sites.

**Keywords:** consensus sequence, information theory, sequence logo, sequence walker, binding site, genetic control

*All models are wrong but some are useful.*

GEORGE EP BOX 1979, p 202

## How to be sure to make a mistake

Genes are controlled by proteins that bind to specific spots on the DNA sequence. Molecular biologists often represent the patterns at these spots by using a consensus sequence. For example, after aligning some binding sites so that they match each other, one position might contain 70% adenine, 10% cytosine, 10% guanine and 10% thymine. The consensus is the most frequent base, 'A'. This is the simplest (and possibly the most commonly applied) approach, but there are alternatives (Day and McMorris 1992). Various kinds of consensus sequence commonly found in the molecular biology literature will be considered here, while the controversy over the use of consensus *trees* used in phylogenetic inference (Barrett et al 1991; Nelson 1993; Barrett et al 1993; de Queiroz 1993) will not be covered.

The main difficulty with using consensus sequences is that they present distorted pictures of binding sites. To locate new binding sites, consensus sequences are compared to various locations in a sequence and the number of matches is tallied. A difficulty arises because a position that is always an 'A' in the original set is treated the same as a position that is just 70% A. If we think that a position has A, then when we use this observation to look for additional binding sites, we will find mismatches for 30% of the acceptable sequences. This problem is compounded across the entire binding site, which may be 20 or even 40 bases long (Schneider 1996; Zheng et al 1999). For example, a commonly cited consensus sequence is TA TAA T (Lewin 1997), which represents the -10 region of bacterial promoters originally discovered by David Pribnow (1975).

The most prominent bases for the boxed positions are only 49%, 58% and 54% respectively (Lisser and Margalit 1993). If one demands that a site have all of the consensus bases, one finds only 14 TATAAT sequences out of 291 sequences in the database. To deal with this, people often count mismatches, but it is not obvious from the simple consensus which bases are allowed to be more variable. Sometimes variations such as allowing C or G are indicated but, again, the degree of allowed variation is lost. It is not surprising then, that consensus sequences frequently fail to identify binding sites or that they predict sites where there are none.

Consensus sequences have other serious problems, many of which are revealed by using information theory to measure the amount of conservation in bits. In a set of aligned binding sites, a DNA position that is always an A stays that way during evolution because the molecule that binds to it always selects A from the four possible bases (Schneider 2000). Such a selection can be made with a minimum of two yes-no questions: 'Is it in the set A or T?' and 'Is it in the set A or C?', so the selection takes two bits of information, one to answer each question. Likewise, a position that is either A or T only requires one yes-no question – the other one being ignored – so has one bit of sequence conservation. The late Claude Shannon figured out how to consistently measure the average information when the frequencies are not so simple (Shannon 1948; Schneider et al 1986; Schneider 1995). One can plot the sequence conservation across all positions in the set of aligned binding sites. This continuous quantitative measure

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often follows a sine wave, reflecting the binding of a protein to one face of helically twisting B-form DNA (Papp et al 1993; Schneider 1996; Schneider 2001). This subtle effect cannot be seen by using consensus sequences.

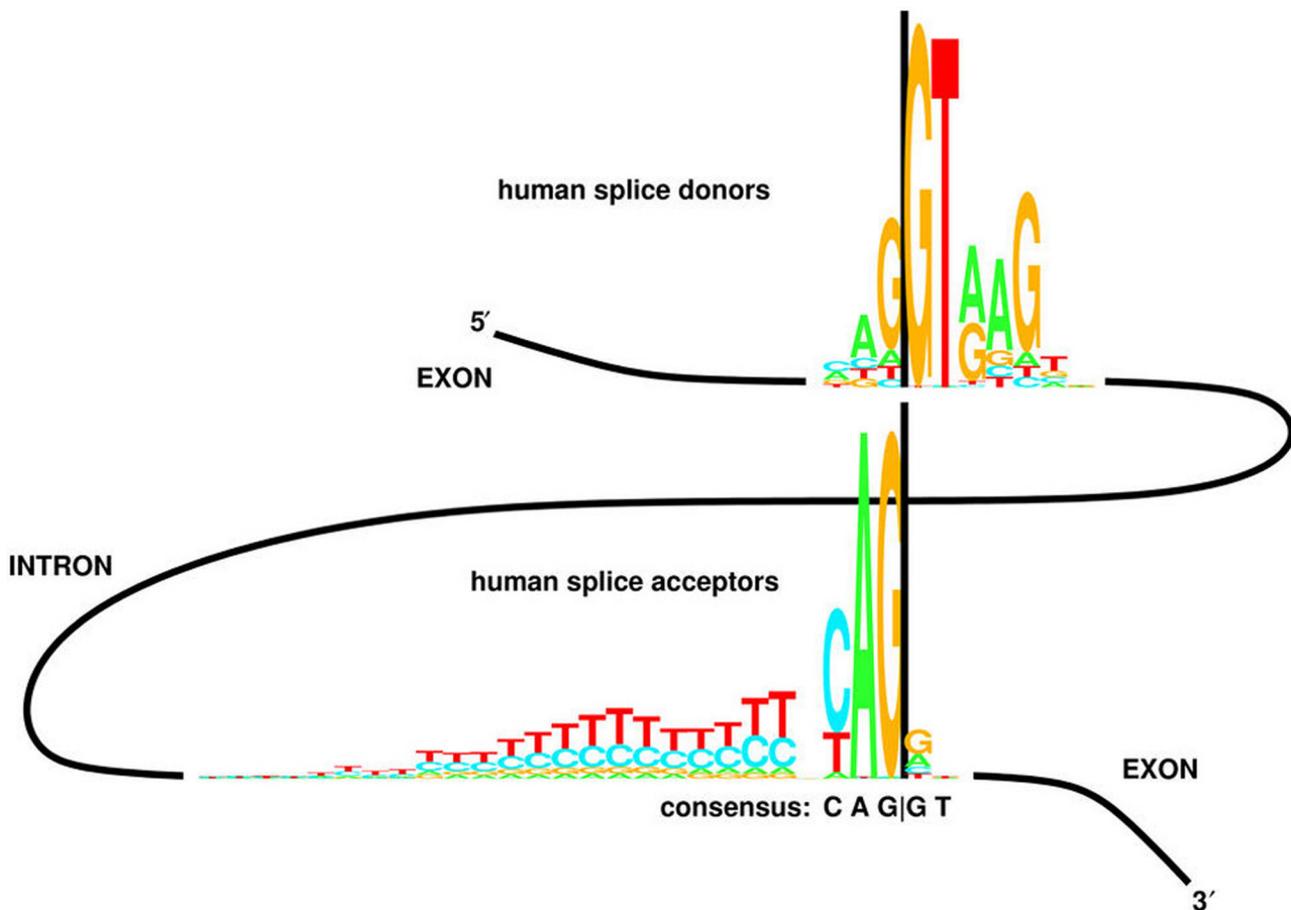
## A paradox: how can two things be the same but different?

Intriguingly, the binding sites for human splice junction donor and acceptor sites have the same consensus sequence for a portion of each site around the junction. Yet, when we measured the sequence conservation in bits we found that the information curves are quite different (Stephens and Schneider 1992). How could two sites have the same consensus sequence but be different? This conundrum led us to introduce a computer graphic, called a sequence logo, in order to understand the difference (Figure 1). A logo depicts an average picture of the set of binding sites by a series of stacks of letters. The height of each stack is the sequence conservation (measured in bits of information; the vertical black bar at each junction is 2 bits high) and the

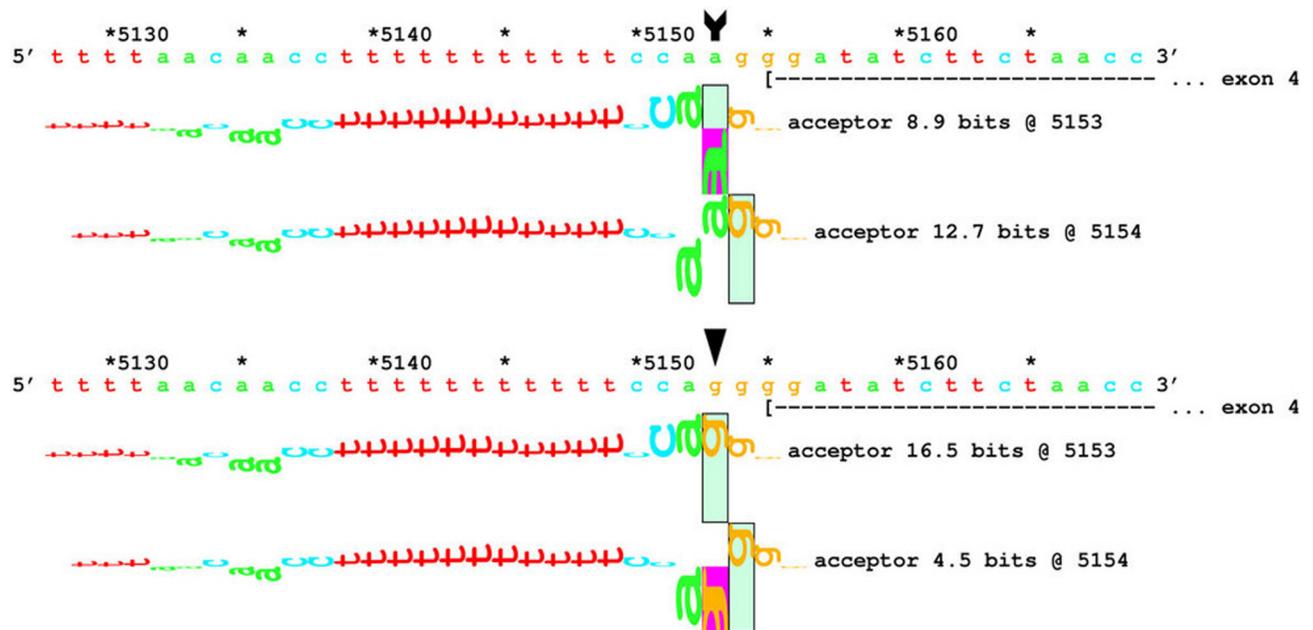
heights of the letters show the relative proportions of the bases, sorted so that the more frequent bases are on top. From the logos shown, it is clear that the donor and acceptor sites have different ‘emphasis’, but this cannot be seen with the consensus sequence CAG|GT, which matches both of them at the junction. The difference in emphasis is important because it shows that there is more information on the intron side of each junction. This allows more freedom during the evolution of the protein-coding exon side, which is a biologically sensible result. The resemblance between the two junctions suggests that the splice machinery that binds to donors and acceptors have a common ancestor (Stephens and Schneider 1992).

## Walking along the genome

One can depict individual sites using another graphic called a sequence walker, in which the height of a letter above or below zero shows how much that base contributes to the average sequence conservation of the entire collection of sites shown in the logo (Figure 2) (Schneider 1997b;



**Figure 1** Sequence logos (Schneider and Stephens 1990) for human donor and acceptor splice junctions (Stephens and Schneider 1992) compared to the consensus sequence for both sites. Source: Adapted from Stephens and Schneider (1992).



**Figure 2** Sequence walkers (Schneider 1997b) for a human acceptor site in the iduronidase synthetase gene and a mutation (indicated by an arrow). On the top sequence, the normal end of exon 4 is shown by a bracket and dashed line. The vertical rectangle on a sequence walker is the 'zero base' used to identify the location of the walker. The vertical rectangles also indicate a scale from  $-3$  to  $+2$  bits. A 12.7 bit acceptor at 5154 directs splicing to the correct location. Source: Adapted from Rogan et al (1998).

Schneider 1997a). Instead of counting matches to a consensus, one sums the information contributions for a given sequence to obtain the information for an individual binding site. (The Shannon information measure is unique in that it is the only measure that allows addition for statistically independent components (Shannon 1948). Generally, binding site bases are independent (Stephens and Schneider 1992).)

Sequence walkers can be stepped along the sequence (hence the name) to discover positions that match a particular model, and one can predict whether or not a sequence change will destroy the site and cause a genetic disease (Rogan et al 1998). In the case shown, splicing is normally accomplished using a 12.7 bit acceptor at position 5154. Nearby, however, is an 8.9 bit 'cryptic' acceptor that is not used apparently because the strongest site in any local region normally wins the competition for splice factors. An A to G mutation at 5153 destroys the normal site, making it 4.5 bits while simultaneously raising the cryptic site to 16.5 bits. This results in a single base frame shift, the loss of the protein, and Hunter disease. Cases like this are difficult to understand using consensus sequences because sites are affected by all of their parts and quantitative differences are missed. Using information theory and sequence walkers we have interpreted about 100 mutations in two human workdays (the computer time is only a few seconds).

## Statistical effects of making a consensus

The overall strength of a binding site is found by summing the individual bit contributions. A distribution of these strengths is roughly Gaussian and shows that most natural binding sites have much less information than the consensus sequence (Schneider 1997a). The strict consensus (where only the most frequent base is used) is the strongest possible binding site and is on the far high end of the distribution. For example, only one in 270 acceptor sites matches the strict consensus. For this reason it is generally inappropriate to say that one has a consensus binding site at such-and-such a position on a sequence.

As mentioned earlier, using consensus sequences to find binding sites by counting mismatches can lead to errors. How does this compare to the information theory approach? If matches to the consensus are assigned to have 1 unit and mismatches 0 units, then the total count is an integer. In contrast, the information theory weights are  $2 + \log_2(\text{base frequency}) + (\text{a small-sample correction})$ , which includes the real numbers. Summing the information theory weights gives continuous results, while counting mismatches gives blocky results that will often be off the mark. The commonly used 'percent identity' between two sequences, such as proteins, is flawed for the same reasons.

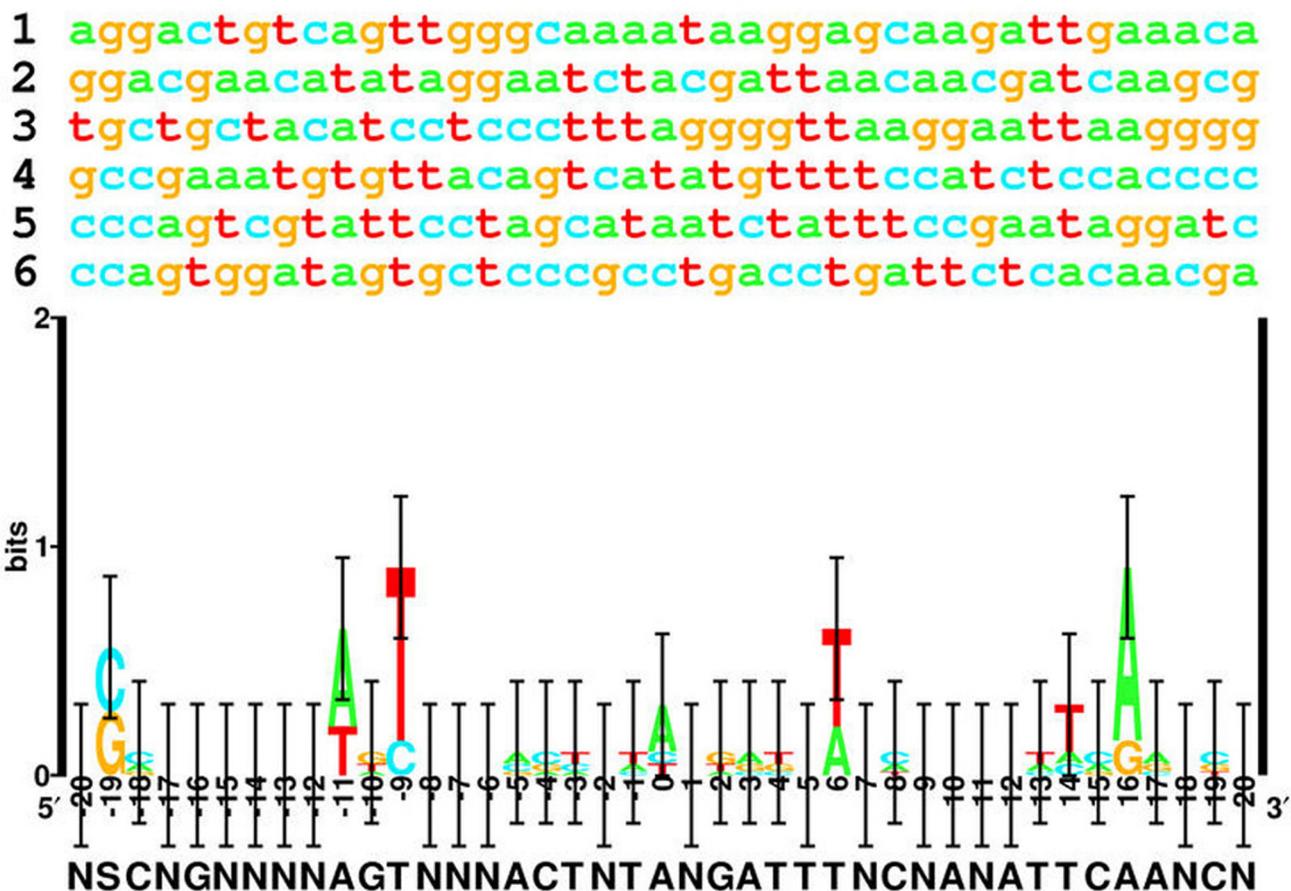
Sometimes counting matches or mismatches can give results opposite to the information measure weights so that a base in a site could have a mismatch to the consensus and yet that base could contribute positive information. For example, for a position that has 60% A, 30% T, 5% G, and 5% C the consensus base is A by two-fold, and yet a T in an individual binding site would contribute  $2 + \log_2 0.30 = 0.26$  bits. Only by noting the total distribution can we learn that the T contributes positively to the information. A related effect that is hidden by a consensus is that the diversity of the less frequent bases affects the total sequence conservation. For example, a position with 70% A, 30% T, 0% G, and 0% C has 1.12 bits of conservation, but a position with 70% A and 10% for each of C, G and T has only 0.64 bits. The consensus for both cases, A, does not distinguish between these.

When there are very few sequences, statistical artifacts crop up. Even if there's no information in the set, it can look like there is. For example, if one has only 6 random sequences, one will frequently observe positions that have 50% or more of one base. If, as is commonly done, one uses 50% as the cutoff for writing the consensus base, then one can get the false impression that there is pretty good sequence conservation. In the example shown in Figure 3, 25 of 41 positions would be identified as 'conserved' even though the sequences were randomly generated! In general,  $26 \pm 3$  of the 41 positions in 6 randomly generated sequences would be marked as the consensus.

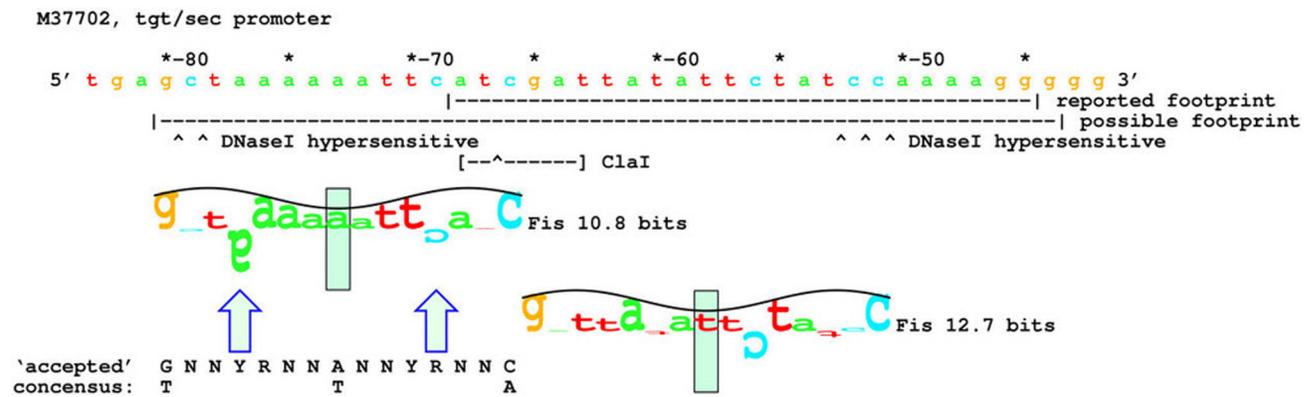
### Missing the trees in the data forest

As a result of counting mismatches to a consensus it is possible to entirely miss a binding site. One of the most

## 6 random sequences



**Figure 3** Sequence logo for random sequences. Error bars, shown by I beams, indicate one standard deviation of the stack height. Note that a small-sample correction (Schneider et al 1986) suppresses the stack height so that a position such as -19, which is 50% C and 50% G, is lower than 1 bit. The correction is needed to counter a statistical bias that causes an apparent information to appear when one substitutes frequencies for probabilities in Shannon's equation (Schneider et al 1986; Miller 1955; Basharin 1959). The same effect makes one tend to see patterns where there are none. The consensus sequence on the bottom was chosen from positions that have 50% or more of one base. S is the two-letter code for C or G.



**Figure 4** Region upstream of the *tgt/sec* promoter of *E. coli* analyzed by Fis sequence walkers. The information for each Fis site was computed from models that are 21 bases wide (-10 to +10) but only the range -7 to +7 is shown by walkers. The sine waves represent major (peaks) and minor (valley) grooves faced by the Fis protein. Source: Adapted from Schneider (1997b).

striking examples is a Fis site in the *tgt/sec* promoter of *E. coli* (Figure 4). We carefully collected 60 sequences shown by DNase I footprinting to be bound by Fis, used information theory to maximize the information content of the alignment (Schneider and Mastronarde 1996) and produced a model of how Fis binds (Hengen et al 1997). The model did a good job of predicting where Fis binds in the original footprint regions. However the model also predicted a site in *tgt/sec* that was not noted by the original authors. Surprisingly, four pieces of data support the existence of a Fis site centered at position -73 relative to the start of transcription (Slany and Kersten 1992):

1. Fis often induces DNase I hypersensitive phosphates; these are seen between bases -53 and -50, corresponding to the Fis site at position -58. In addition there are hypersensitive positions between -80 and -78, which correspond to the site shown by the walker at -73.
2. The 5' end of the original DNase I footprints was not well determined, but could have extended to cover the Fis site at -73.
3. Gel mobility shift assays showed two band shifts when the entire region was used, one band shift when the region 5' to the conveniently (!) placed *Cl*I site was removed (which would eliminate the proposed Fis site) and none when both were removed.
4. Assays with these same nested DNAs showed that both sites activate transcription.

The authors were aware that there was a second binding site, but placed its location somewhere in the 69 bases upstream of the *Cl*I site. Why did they miss the site? Two positions (indicated by arrows in the figure) did not match the 'accepted' consensus sequence (Hübner and Arber 1989). The consensus method gave these positions far more

weight than was appropriate. The information for the site at -73 is 10.8 bits, which is 2 bits more than the average. To determine if there is really a site there, we performed a gel shift experiment using a DNA containing only the proposed Fis site at -73 and showed that the sequence is indeed bound by Fis (Hengen et al 1997). Because the consensus sequence failed to predict a site that had been documented experimentally, that site could not be seen, and to the scientists it did not exist (Kuhn 1970).

A more critical example is in the *hMSH2* gene, which is associated with familial nonpolyposis colon cancer (Rogan and Schneider 1995). A 'T' to 'C' transition occurred at position -5 of an acceptor site and this change was proposed to be the cause of the disease (Fishel et al 1993). Inspection of the logo in Figure 1 shows that the consensus at position -5 (base zero is just to the left of the vertical bar, the first base on the intron side) is a T, but that close to half of the bases in the polypyrimidine tract are C. When the transition is made, the individual information changes by only 0.2 bits, which is not significantly different. A study of 20 normal people found that only 2 had this change (Leach et al 1993), so the change is a polymorphism unrelated to the disease.

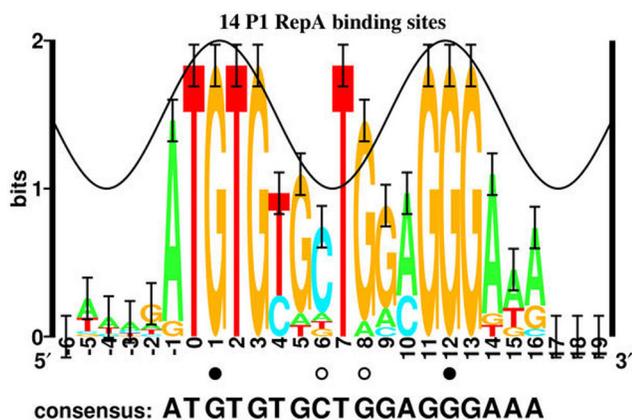
Why did this potential 'misdiagnosis' happen? We suppose that T was taken to be the consensus sequence. Given this, one would interpret *any* change from that consensus to be detrimental. In this case the consensus sequence was so rigid that it could not handle a subtle change and a site disappeared from the scientist's view even though it was still functional. As DNA sequencing technologies become widely available to doctors, this situation will come up repeatedly. Serious malpractice suits could occur as a result of using the consensus model.

## Flipping the light on to see an unseen world

Two recently published examples demonstrate some of the interesting biology that one can miss by using a consensus sequence. The first example is the RepA binding site (Figure 5). The sine wave over the logo represents the twist of B-form DNA. The crests of the wave represent the protein facing a major groove and the troughs represent the protein facing a minor groove. Experimental data indicate that the major groove sides of Gs at positions 1 and 12 (black dots) are facing the protein, while the major groove sides of those base pairs at positions 6 and 8 (open circles) are facing away from the protein (Papp et al 1993). Hydroxyl radical and ethylation interference data also support this assignment and indicate that RepA binds to only one face of the DNA (Papp and Chatteraj 1994).

RepA and other DNA binding proteins show sequence conservation up to 2 bits where they contact the major groove and only 1 bit where they face a minor groove (Papp et al 1993; Schneider 2001). The upper bound of 2 bits is achievable because all 4 bases can be distinguished using contacts in the major groove (Seeman et al 1976). In contrast, the minor groove of B-form DNA is essentially symmetrical and can only provide up to 1 bit of sequence conservation.

Intriguingly, as seen in Figure 5, RepA violates this rule at positions +7 and +8 where the protein faces a minor groove (Papp et al 1993). The violation implies that the DNA is not B-form. To understand this anomaly, we substituted a variety of chemically modified base pairs at position +7 (and its complement +7') and found that the N3 proton on the thymine is responsible for contacting RepA



**Figure 5** Sequence logo for RepA binding sites. Error bars indicate standard deviations of the entire stack height. Source: Adapted from Schneider (2001).

through the minor groove (Lyakhov et al 2001). Since the N3 proton is normally sequestered in the center of the DNA helix, the DNA must indeed be distorted, as predicted from the sequence logo. Furthermore, the acceptable contact points for hydrogen bonding vary by several angstroms more than an H-bond could withstand in a rigid structure, suggesting that the base may rotate towards the minor groove for binding to occur. In other words, the T at +7 may be ‘flipping’ out of the DNA.

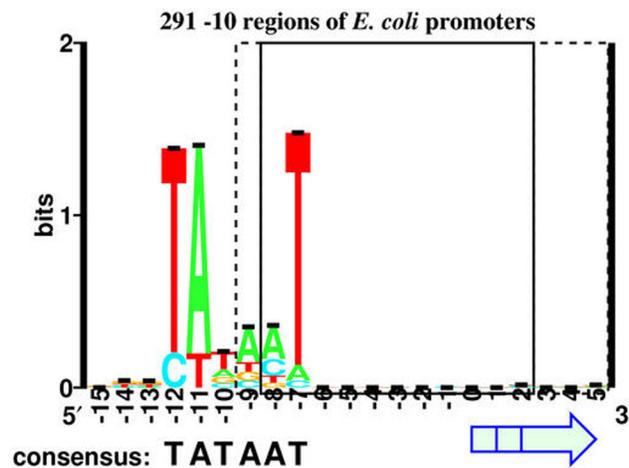
Base flipping was discovered by Rich Roberts in the co-crystal of the *HhaI* methyltransferase (Roberts 1995; Roberts and Cheng 1998). This solved a puzzle of how that enzyme functions, since the chemistry of methylation requires attack from above or below the plane of the base. Such an attack is not possible inside the DNA helix. The *HhaI* methyltransferase solves the problem by flipping the base out of the helix and into a pocket of the enzyme. Other DNA modification proteins also flip bases (Cheng et al 1993; Klimašauskas et al 1994; Verdine 1994; Reinisch et al 1995).

Why would RepA be flipping a base? RepA is used by the bacteriophage P1 plasmid for DNA replication (Abeles 1986; Abeles et al 1989). DNA replication requires that the helix be opened before synthesis can begin. The first step of this process would be the binding of RepA to the DNA. A very simple second step would be the flipping of a base out of the DNA, since DNA ‘breathing’ occurs naturally on a millisecond scale (Guéron et al 1987; Leroy et al 1988). If the thymine at +7 flips, is captured, and then held out of the DNA helix by RepA, weakened stacking could allow the remainder of the DNA to be more easily opened by a DNA helicase.

Sequence logos of other DNA replication protein binding sites have similar anomalies (Schneider 2001), suggesting that base flipping may be a general mechanism for the second step of DNA replication.

How is this related to consensus sequences? The consensus sequence for RepA sites can be determined by reading the top letters of the sequence logo (Figure 5) because the letters are sorted so that the most frequent base is on top. One finds: 5' ATGTGTGCTGGAGGGAAA 3'. By viewing the binding site through the restrictive glasses of a consensus sequence, the unusual base becomes indistinguishable from the other bases!

A second example is the TATAAT sites mentioned earlier, for which the sequence logo is shown in Figure 6. The logo shows that there is much lower sequence conservation in positions -10, -9 and -8 than in positions -12, -11 and -7, but



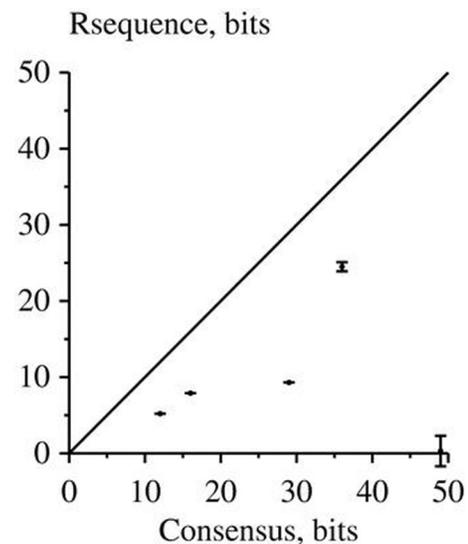
**Figure 6** Sequence logo for the  $-10$  region of *E. coli* promoters. The promoters were from the Lisser-Margalit database (Lisser and Margalit 1993). The dashed and solid boxes show the regions opened by the polymerase, while the arrow shows the start points of transcription. Source: Adapted from Schneider (2001).

the low region is significantly above background since the error bars are so small. (Contrast these tiny error bars to the ones in Figure 3 and Figure 5, where there are fewer sites.) The DNA region opened by RNA polymerase straddles the gap, leaving a highly conserved T at  $-7$  near the 5' edge of the opened region. We propose that  $-7$  is the first base opened during RNA transcriptional initiation, and a reasonably large body of experimental evidence supports this hypothesis (Schneider 2001). As with RepA sites, the unusual thymine is obscured if one uses the consensus sequence.

### Just say no!

We can express a consensus sequence in bits and so quantify the effect of making one. Each unique base (A, C, G or T) of a consensus counts as 2 bits. When two variations such as C or G are allowed (eg Figure 3) we count 1 bit; there is, of course, no small-sample correction. 3 bases would count

as  $2 - \log_2 3$  (Schneider et al 1986), and 4 bases (N) would be zero. Plotting the total information of each sequence logo shown in this paper against this 'consensus information' we obtain Figure 7 (summarized in Table 1). The figure shows that the consensus is always larger than the information content, even drastically so. However, the consensus could be tweaked (in individual cases) by arbitrarily playing around with the rules (Day and McMorris 1992) to reduce the number of bits. But all the tweaking in the world will never give the proper weights because the frequencies are always rounded to obtain a consensus sequence. The examples in this paper show that when faced with the prospect of using a consensus sequence, we should 'just say no'.



**Figure 7** Consensus versus  $R_{sequence}$ . The information for the 5 sequence logos in figures 1,3,5 and 6 was graphed by comparing the information content ( $R_{sequence}$ ) to the information content of the corresponding consensus sequence.  $R_{sequence}$  is the average information in a set of binding sites. It is also the summed area under the sequence logo. The line at  $45^\circ$  represents equality between the two measures. The data are summarized in Table 1.

**Table 1**  $R_{sequence}$  and consensus information for sequence logos.  $R_s$  is  $R_{sequence}$ ;  $SD$  is the standard deviation of  $R_s$  (to one decimal place);  $CON$  is the consensus information. The range of the site used is shown in columns From and To. The lowest frequency for using a base in each consensus was 0.4 and the consensus was computed using the program consensus (version 1.16, <http://www.lecb.ncifcrf.gov/~toms/delila/consensus.html>)

Name	$R_s$ bits	$SD$ bits	$CON$ bits	Consensus	From	To
donor	7.9	0.0	16	NAGGTAAGTN	-3	+6
acceptor	9.3	0.0	29	NNNNNNNNNTTTTTTTTTCAGGN	-25	+2
random	0.3	2.0	49	NSCNGNNNNAGTNNNACTNTANGATTTNCNANATTCAANCN	-20	+20
repa	24.5	0.6	36	ATGTGTGCTGGAGGGAAA	-1	+16
-10	5.2	0.0	12	TATAAT	-12	-7

## Models and illusions

One sometimes reads about how a particular DNA sequence has a consensus sequence at such-and-such a position (Robberson et al 1990). Thus using consensus sequences has led these biologists into a philosophical trap: confounding the model of reality (the consensus sequence) with reality (the binding sites). Even the original title of our paper on sequence logos reflects our initial confusion on this issue (Schneider and Stephens 1990). Logos and walkers let us see more deeply into the genetic structure, revealing the details of sites and how mutations work. But no matter how sophisticated we are in depicting the patterns at binding sites, all we have are models. Logos and walkers are clearly better than consensus sequences (and can replace them completely), but they are still only representations of the universe 'out there' (Box 1979). It is surprising, then, that scientists forget this and treat the consensus as reality. The effect was understood more than 30 years ago by Thomas Kuhn: once a paradigm is formed it occludes other ways of thinking and molds the way scientists perceive the world (Kuhn 1970). Yet a consensus can no more be 'in' a DNA sequence than the meaning of these words is on the page. These words are interpretations in your mind; the page only has some disconnected black squiggles. One way to see this is to consider the perennial myth of a face on Mars that appears in American tabloid magazines. Whether or not there is a face on Mars, most of us have seen faces in clouds. Are there really faces there? Evidently not. Experiments with sheep and monkeys have identified neurons that become excited when a face is presented in the visual field (Kendrick and Baldwin 1987). So faces in clouds, words, and consensus sequences are all constructs in our brains. Stranger still, the words may not be there when you perceive them since neural impulses take 300 milliseconds to travel from your eye to your brain (Rager and Singer 1998), where, after another 80 milliseconds, they are finally perceived (Eagleman and Sejnowski 2000). All that we see, hear, feel, smell and taste is delayed, so the entire perceived world is a model in our minds. Optical illusions remind us, and Zen masters understood that everything is illusion (Purves et al 2002).

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